# Mathematics I Standards for Mathematical Practice and TEAM 

The Standards for Mathematical Practice describe varieties of expertise that mathematics educators at all levels should seek to develop in their students. These practices rest on important "processes and proficiencies" with longstanding importance in mathematics education. The first of these are the NCTM process standards of problem solving, reasoning and proof, communication, representation, and connections. The second are the strands of mathematical proficiency specified in the National Research Council's report Adding It Up: adaptive reasoning, strategic competence, conceptual understanding (comprehension of mathematical concepts, operations and relations), procedural fluency (skill in carrying out procedures flexibly, accurately, efficiently and appropriately), and productive disposition (habitual inclination to see mathematics as sensible, useful, and worthwhile, coupled with a belief in diligence and one's own efficacy).

## 1. Make sense of problems and persevere in solving them.

Mathematically proficient students start by explaining to themselves the meaning of a problem and looking for entry points to its solution. They analyze givens, constraints, relationships, and goals. (1) They make conjectures about the form and meaning of the solution(3) and plan a solution pathway rather than simply jumping into a solution attempt. They consider analogous problems, and try special cases and simpler forms of the original problem (5) in order to gain insight into its solution. They monitor and evaluate their progress and change course if necessary. Older Students might, depending on the context of the problem, transform algebraic expressions or change the viewing window on their graphing calculator to get the information they need. Mathematically proficient students can explain correspondences between equations, verbal descriptions, tables, and graphs or draw diagrams of important features and relationships, graph data, and search for regularity or trends, Younger students might rely on using concrete objects or pictures to help conceptualize and solve a problem. Mathematically proficient students check their answers to problems using a different method, and they continually ask themselves, "Does this make sense?" They can understand the approaches of others to solving complex problems and identify correspondences between different approaches.(3)

Activities and Materials

## Questioning

Academic Feedback

Thinking
Problem Solving
Expectations
*Assessment
*Student Work

## 2. Reason abstractly and quantitatively.

Mathematically proficient students make sense of quantities and their relationships in problem situations. (5) They bring two complementary abilities to bear on problems involving quantitative relationships: the ability to decontextualize-to abstract a given situation and represent it symbolically (1) and manipulate the representing symbols as if they have a life of their own, (9) without necessarily attending to their referents-and the ability to contextualize, to pause as needed during the manipulation process in order to probe into the referents for the symbols involved. (7) Quantitative reasoning entails habits of creating a coherent representation of the problem at hand; (3) considering the units involved; attending to the meaning of quantities, (2) not just how to compute them; and knowing and flexibly using different properties of operations and objects.(8)

Thinking
Problem Solving
*Assessment
*Student Work

## 3. Construct viable arguments and critique the reasoning of others.

Mathematically proficient students understand and use stated assumptions, definitions, and previously established results in constructing arguments. They make conjectures and build a logical progression of statements to explore the truth of their conjectures. (5) They are able to analyze situations by breaking them into cases,(2) and can recognize and use counter examples.(8) They justify their conclusions, (3) communicate them to others, and respond to the arguments of others. They reason inductively about data, (1) making plausible arguments that take in account the context from which the data arose. Mathematically proficient students are also able to compare the effectiveness of two plausible arguments, (1) distinguish correct logic or reasoning from that which is flawed,(5) and-if there is a flaw in an argument-explain what it is. Elementary students can construct arguments using concrete referents such as objects, drawings, diagrams, and actions. Such arguments can make sense and be correct, even though they are not generalized or made formal until later grades. Later, students learn to determine domains to which an argument applies. (2) Students at all grades can listen or read the arguments of others, decide whether they make sense,(3) and ask useful questions to clarify or improve the arguments.

## Motivating Students

Questioning
Academic Feedback
Thinking
Problem Solving
*Assessment

Standards and
Objectives
Assessment
Questioning
Thinking
Problem Solving
Student Work

Activities and Materials

Thinking
Problem Solving
*Assessment
*Student Work

## 6. Attend to precision.

Mathematically proficient students try to communicate precisely to others. They try to use clear definitions in discussion with others and in their own reasoning. They state the meaning of the symbols they choose, including using the equal sign consistently and appropriately. They are careful about specifying units of measure, and labeling axes to clarify the correspondence with quantities in a problem. They calculate accurately and efficiently, express numerical answers with a degree of precision appropriate for the problem context.(7) In the elementary grades, students give carefully formulated explanations to each other. By the time they reach high school they have learned to examine claims and make explicit use of definitions.(1)

Academic Feedback

## Student Work

Presenting Instructional Content

Thinking
Problem Solving
*Assessment
$\times$

## 7. Look for and make use of structure.

Mathematically proficient students look closely to discern a pattern or structure.(1) Young students, for example, might notice that three and seven more is the same amount as seven and three more, or they may sort a collection of shapes according to how many sides the shapes have. Later, students will see $7 \times 8$ equals the well remembered $7 \times 5+7 \times 3$, in preparation for learning about the distributive property. In the expression $x 2+9 x+14$, older students can see the 14 as $2 \times 7$ and the 9 as $2+7$. They recognize the significance of an existing line in a geometric figure (1) and can use the strategy of drawing an auxiliary line for solving problems. They also can step back for an overview and shift perspective. (9) They can see complicated things, such as some algebraic expressions, as single objects or as being composed of several objects.(1) For example, they can see $5-3(x-y) 2$ as 5 minus a positive number times a square and use that to realize that its value cannot be more than 5 for any real numbers $x$ and $y$.

Activities and Materials Thinking

Problem Solving
*Assessment
*Student Work

## 8. Look for and express regularity in repeated reasoning.

Mathematically proficient students notice if calculations are repeated, (1) and look both for general methods and for shortcuts. (5) Upper elementary students might notice when dividing 25 by 11 that they are repeating the same calculations over and over again,(7) and conclude they have a repeating decimal.(3) By paying attention to the calculation of slope as they repeatedly check whether points are on the line through $(1,2)$ with slope 3 , middle school students might abstract the equation $(y-2) /(x-1)=3$. (1) Noticing the regularity in the way terms cancel when expanding $(x-1)(x+1),(x-1)(x 2+x+1)$, and $(x-1)\left(x 3+x^{2}+x+1\right)$ might lead them to the general formula for the sum of a geometric series.(8) As they work to solve a problem, mathematically proficient students maintain oversight of the process, while attending to the details. (7) They continually evaluate the reasonableness of their intermediate results.(1)

## Thinking

## Problem Solving

## Student Work

*Assessment
*All standards require student work and assessment though not specifically stated in the description.
**Numbers after Thinking and Problem Solving are referring to specific descriptors indicated in the domain on the TEAM Rubric.

## Modified by R.Pryor from CCSS Math Practices and TEAM for use in Lincoln County Department of Education Professional Learning

